

# Accurate Communication Performance Models of Heterogeneous Clusters: Estimation and Use

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- **Heterogeneous cluster: how to design, estimate and use communication performance model?**

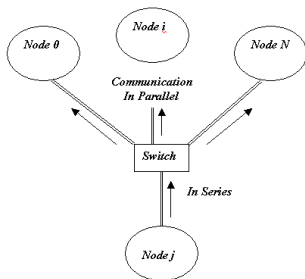
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- **Unable to capture constant and variable contributions of processors and network**
- **Inaccurate to predict communication execution time**

Single-switch cluster

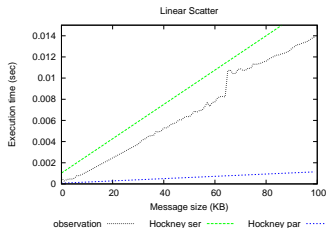


Hockney prediction for linear scatter

Serial:  $T(M, n) = (n - 1)(\alpha + \beta M)$

Parallel:  $T(M, n) = \alpha + \beta M$

$M$  - a message sent to each processor



# Communication Models for Heterogeneous Clusters

## Homogeneous models

*parameters are found by averaging values for all pairs of processors*

- Small number of parameters, compact formulas for collectives
- $O(n^2)$  p2p communication experiments to estimate params
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## Heterogeneous models

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- **Straightforward heterogeneous extension of traditional models**
- **Design of new elaborated heterogeneous models**

# Heterogeneous Extension of Traditional Models

**Hockney**
**Binomial scatter/gather**
**Linear scatter/gather**

fine-grained parallelism

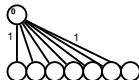
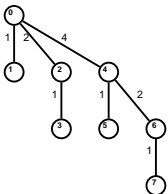
coarse-grained parallelism

**Homogeneous**
 $(\log_2 n)\alpha + (n - 1)\beta M$  - parallel/serial

 $(n - 1)(\alpha + \beta M)$  - serial

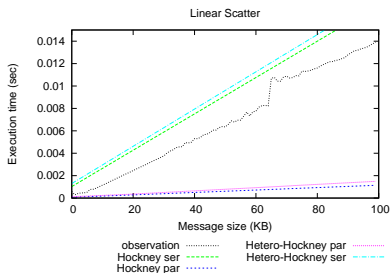
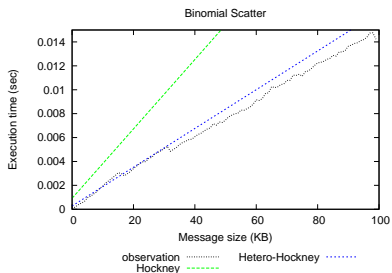
 $\alpha + \beta M$  - parallel

**Heterogeneous**
 $T(k) = \alpha_{rs} + \beta_{rs}2^{k-1}M + \max_{c \in C_{k-1}} T_c(k-1)$ 
 $\sum_{i=0, i \neq r}^{n-1} (\alpha_{ri} + \beta_{ri}M)$  - serial

 $\max_{i=0, i \neq r}^{n-1} (\alpha_{ri} + \beta_{ri}M)$  - parallel


**Implemented heterogeneous extensions: Hockney, LogGP, PLogP**

# Heterogeneous Extension of Traditional Models



# LMO Heterogeneous Communication Model

- **Target platform:** heterogeneous cluster with a single switch

$$i \xrightarrow{M} j: (C_i, t_i) \xrightarrow{(L_{ij}, \beta_{ij})} (C_j, t_j)$$

point-to-point execution time:  $C_i + L_{ij} + C_j + M(t_i + \frac{1}{\beta_{ij}} + t_j)$

$2n$  processor parameters: fixed  $(C_i, C_j)$  and variable  $(t_i, t_j)$  delays

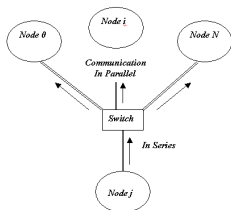
$2C_n^2$  link parameters: latency  $(L_{ij})$  and transmission rate  $(\beta_{ij})$

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More intuitive and accurate predictive formulas:

$$T_{scatter} = (n-1)(C_r + Mt_r) + \max_{i=0, i \neq r}^{n-1} (L_{ri} + \frac{M}{\beta_{ri}} + C_i + Mt_i)$$

How to estimate these parameters?

**Point-to-point experiments are not enough**

# Estimation of Parameters

- Select the communication experiments and express their execution time via the point-to-point parameters
- Measure the execution time of these communications
- Build and solve the system of equations, using the times as a right-hand side values

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- Select the communication experiments and express their execution time via the point-to-point parameters
- Measure the execution time of these communications
- Build and solve the system of equations, using the times as a right-hand side values
- In a triplet of processors ( $i < j < k$ ): 12 unknowns
- Point-to-point communications, roundtrips: 6 independent equations

$$i \xleftrightarrow[M]{M} j \quad T_{ij}(M) = 2(C_i + L_{ij} + C_j + M(t_i + \frac{1}{\beta_{ij}} + t_j)) \quad M := 0, M$$

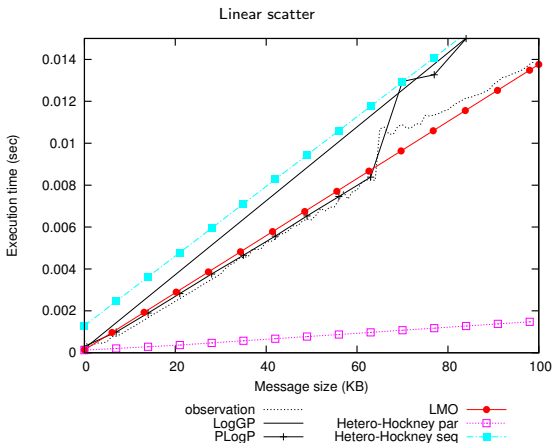
- Linear scatter + linear gather: 6 independent equations

$$i \xleftrightarrow[0]{M} jk = i \xrightarrow{M} jk + i \xleftarrow[0]{} jk$$

$$T_{ijk}(M) = 2(2C_i + Mt_i) + \max_{x=j,k} (2(L_{ix} + C_x) + M(\frac{1}{\beta_{ix}} + t_x))$$

$$M := 0, M$$

# Model Prediction



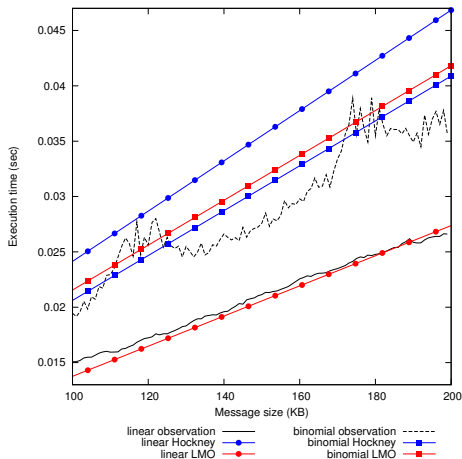


# Model-Based Switch between Algorithms

- Which scatter algorithm is faster for a given message size on a heterogeneous cluster?

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- Hockney: switch to binomial
- LMO: switch to linear



# Model-Based Construction of Communication Trees

## Main approaches

- Mapping of nodes to a tree of a given structure
- Constructing a tree of some structure

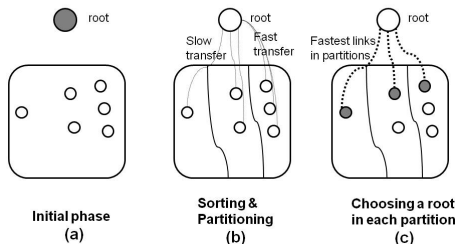
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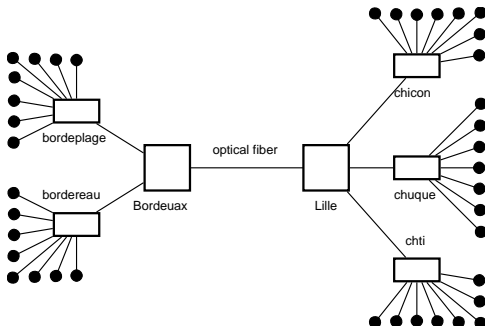
## Example: MPI\_Scatterv/MPI\_Gatherv

- Binomial algorithm - message-unaware, binomial tree  
*fastest-first mapping of nodes: depth-first traverse starting with the lowest-order subtrees*
- Traff algorithm - irregular tree based on message sizes  
*sorting and choosing the roots based on model prediction*



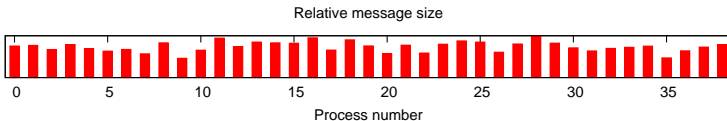
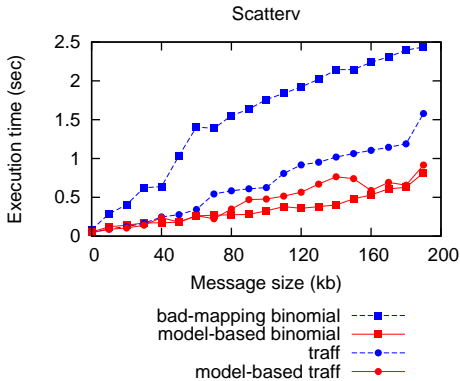
# Experimental Platform: Grid'5000

2 sites, 5 clusters, 40 nodes



MPICH2 over TCP/IP

# Experimental Results: Heterogeneous Hockney



# Ongoing and Future Study

- Communication performance models of hierarchical heterogeneous platforms: interconnected heterogeneous clusters, multicore and multi-GPU clusters
- Optimisation of MPI communication operations on hierarchical heterogeneous platforms
- Application of the proposed approaches to the IBM Exascale platform
- Integration of the proposed approaches into development tools for parallel programming: HeteroMPI, Open MPI

# Publications

## 2011 - 1 conference paper

- Dichev, K., Lastovetsky, A., Rychkov, V. "Improvement of the Bandwidth of Cross-Site MPI Communication Using Optical Fiber", EuroMPI 2011, vol. 6960, Santorini, Greece, Springer, September 18-21, 2011.

## 2010 - 1 journal article, 1 conference paper

- Lastovetsky, A., Rychkov, V., O'Flynn, M. "Accurate Heterogeneous Communication Models and a Software Tool for their Efficient Estimation", International Journal of High Performance Computing Applications, vol. 24, issue 1, pp. 34-48, 2010.
- Dichev, K., Rychkov, V., Lastovetsky, A. "Two Algorithms of Irregular Scatter/Gather Operations for Heterogeneous Platforms", EuroMPI 2010, vol. 6305, Stuttgart, Germany, pp. 289-293, Sep 12-15, 2010.



# Output

**Project web page:** <http://hcl.ucd.ie/project/cpm>

## Software

- 2 packages developed at HCL: MPIBlib, CPM
- Based on system and mathematical software: C/C++, MPI, Autotools, GNU Scientific Library, Boost C++ libraries

## Applications

- Hyperspectral Image Processing (University of Extremadura, Spain)

## Team

- 2 postdoctoral researchers: Vladimir Rychkov, Jun Zhu
- 2 PhD students: Kiril Dichev, Khalid Hasanov

# Collaboration

## Hardware

- Myrinet cluster (Innovative Computing Laboratory, University of Tennessee, USA)
- Grid'5000 (INRIA, CNRS, RENATER, France)

## Collaboration

- David Valencia (University of Extremadura, Spain)
- Shaukat Ali, Rolf Riesen (Exascale Systems, IBM, Ireland)

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UCD CSI



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